A general approach to small-time large deviations for sample paths of infinite dimensional symmetric Dirichlet processes with applications to the Wasserstein diffusion

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Symmetric diffusions on a Polish space can be characterized via local, quasiregular symmetric Dirichlet forms. We define a suitable pointwise intrinsic metric associated to the Dirichlet form which allows us to introduce the notion of energy (with respect to this intrinsic metric) of a sample path.

Under mild assumptions – which imply the necessary exponential tightness – we prove a general small-time sample path large deviation principle for diffusions on a Polish space. As concrete application of this general approach we derive the small time large deviations for the Wasserstein diffusion on the space of probability measures on the unit interval.