On the Chaotic Representation Property of Compensated-Covariation Stable Families of Martingales

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We study the chaotic representation property for certain families \mathcal{X} of square integrable martingales on a finite time interval [0,T]. For this purpose, we introduce the notion of compensated-covariation stability of such families. The chaotic representation property will be defined using iterated integrals with respect to a given family \mathcal{X} of square integrable martingales having deterministic mutual predictable covariation. The main result is: If \mathcal{X} is a compensatedcovariation stable family of square integrable martingales such that $\langle X, Y \rangle$ is deterministic for all $X, Y \in \mathcal{X}$ and, furthermore, the system of monomials generated by \mathcal{X} is total in $L^2(\Omega, \mathcal{F}_T, \mathbb{P})$, then \mathcal{X} possesses the chaotic representation property. We shall then give concrete examples in the case of Lévy processes. This talk is based on a joint paper with H.-J. Engelbert.